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Principles of Software Programming: Basic Algorithms

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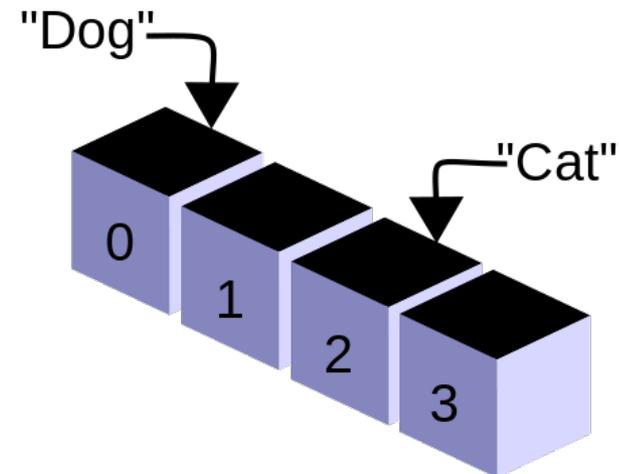
WS 2017

This Episode

- 13:00-16:00
- Data structures:
 - Array
 - Vector
 - Linked list
 - Graph
 - Tree
- Basic Algorithms:
 - Search
 - Sort
 - Recursion

Array

- static (fixed size, does not grow)
- located next to each other in memory

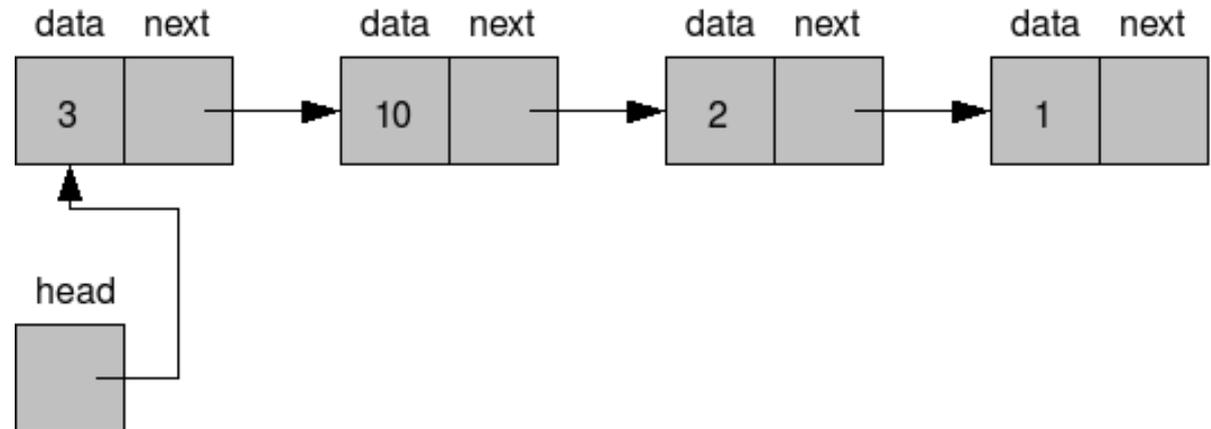


- search: $O(1)$
- insert: $O(N)$
- (memory) space = $n * \text{element size}$
- **vector**: dynamic array (space $\times 2$)

<https://commons.wikimedia.org/wiki/File:CPT-programming-array.svg>

Linked list

- dynamic sequence of nodes (head/tail)
- **singly** linked: each node contains a link to another node
- **doubly** linked: 2 links (next and previous node)
- search: $O(N)$
- insert: $O(N)$
- space >

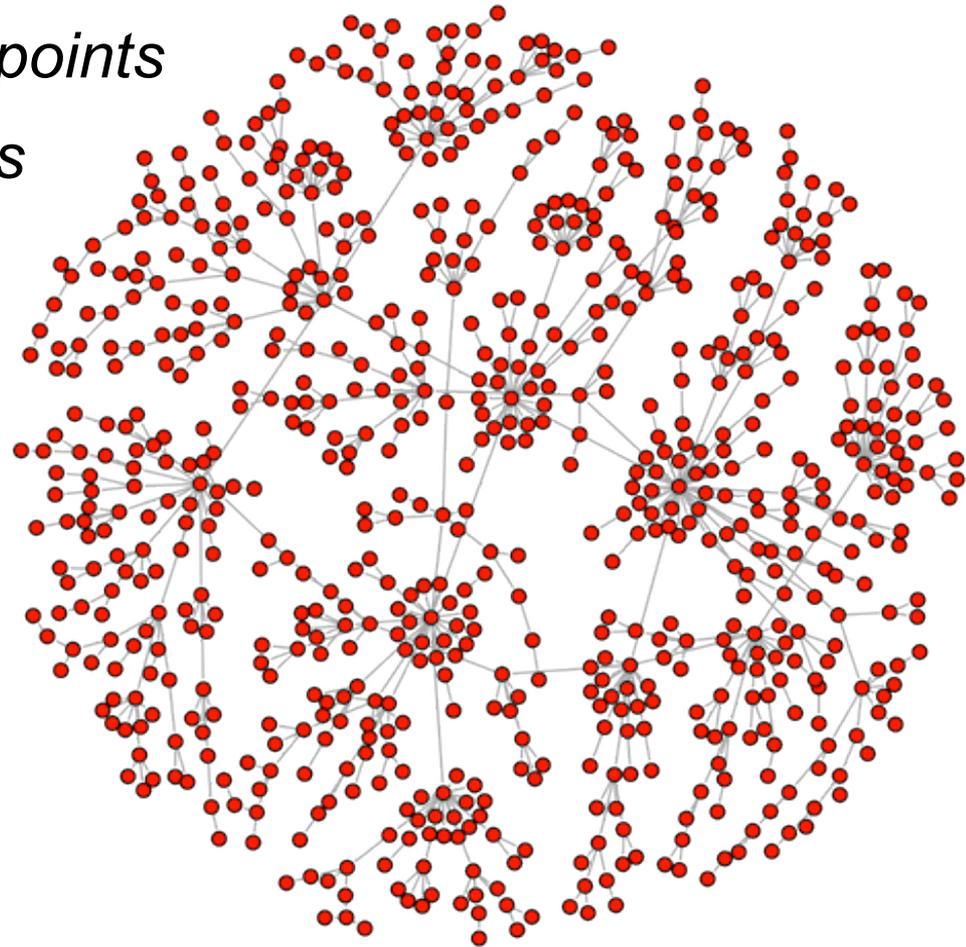


https://commons.wikimedia.org/wiki/File:C_language_linked_list.png

https://en.wikiversity.org/wiki/Data_Structures_and_Algorithms/Arrays,_Lists_and_Vectors

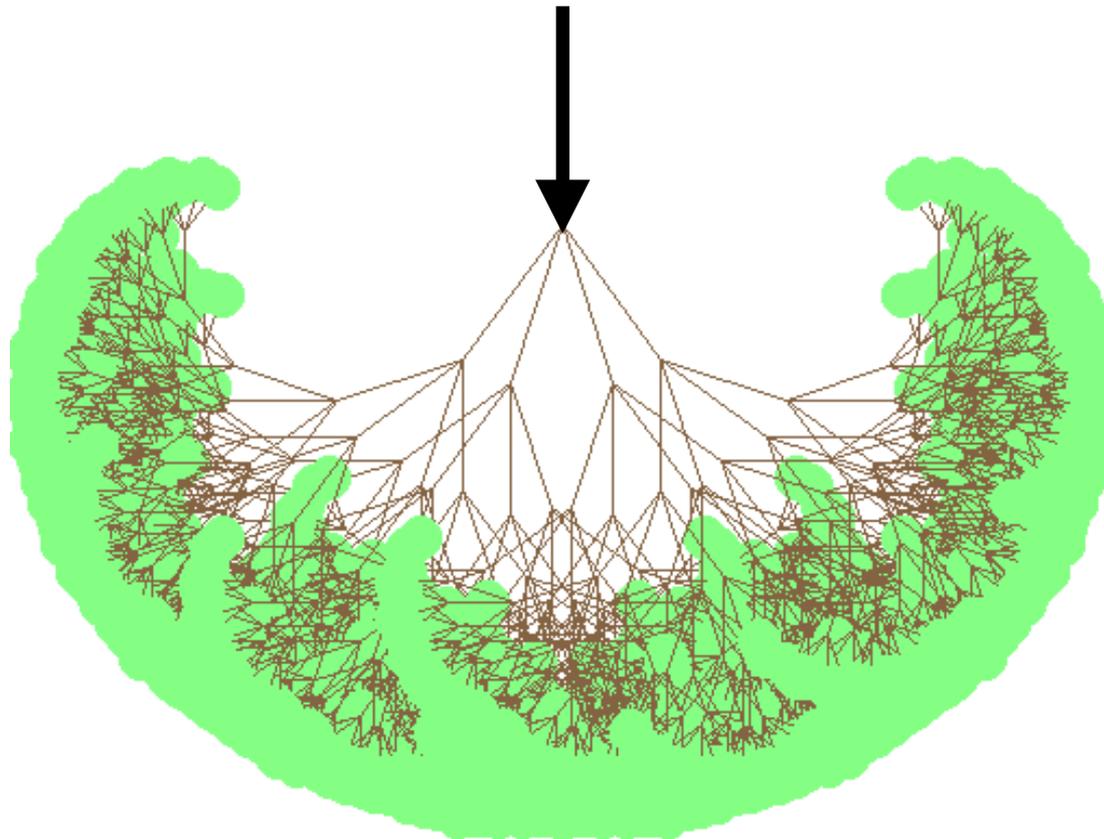
Graph

- $G = (V, E)$
- **set** V of *vertices, nodes or points*
- set E of *edges, arcs or lines*
- *e.g. social network, map,*
- *knowledge graph*



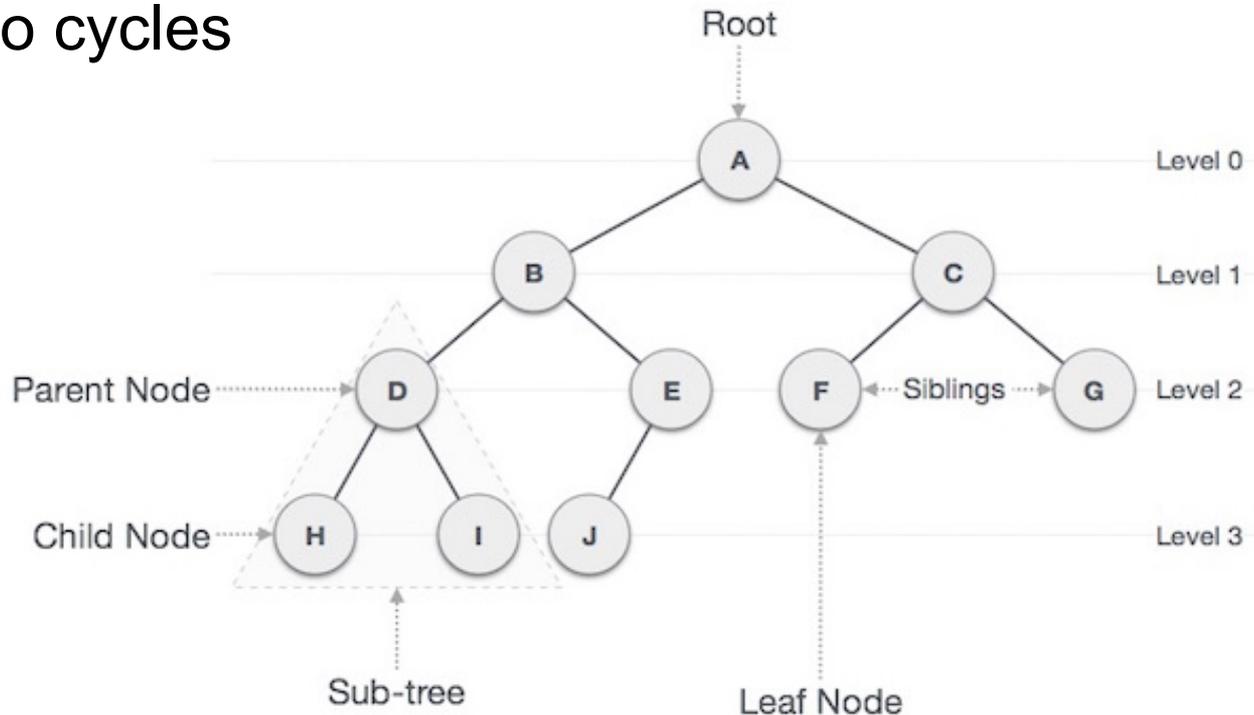
Tree

- is a **rooted** graph with **leaves**

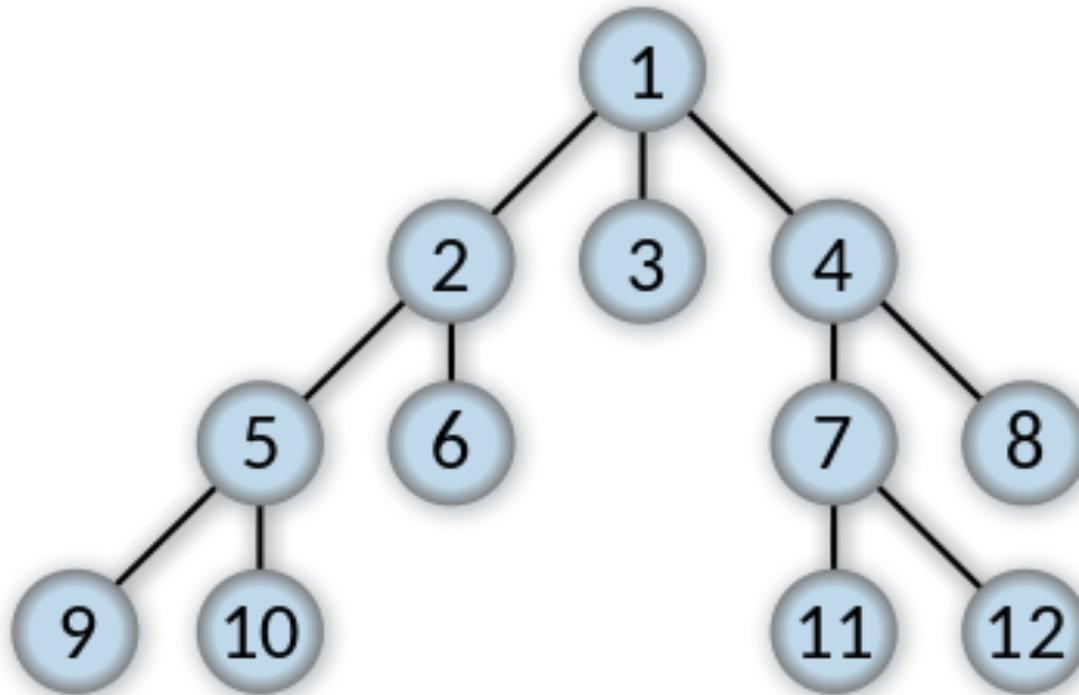


Tree

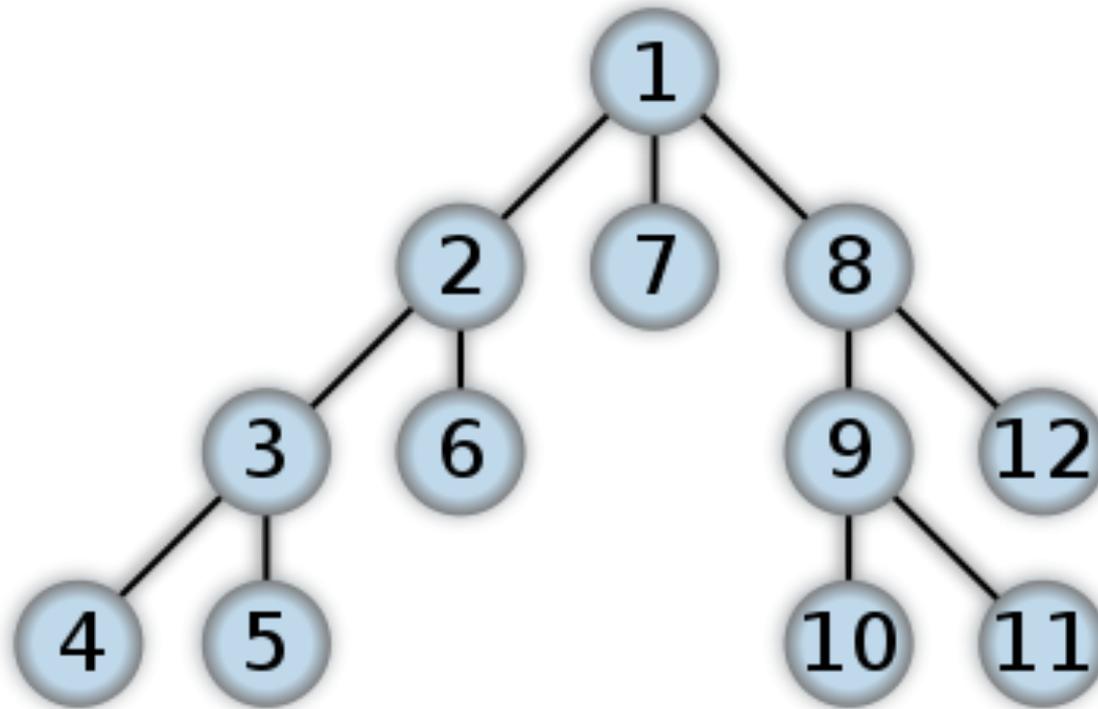
- every **child** node has only one **parent** node
- there is only a single unique **path** between every 2 nodes (path is a sequence of edges that connect 2 nodes)
- contains no cycles



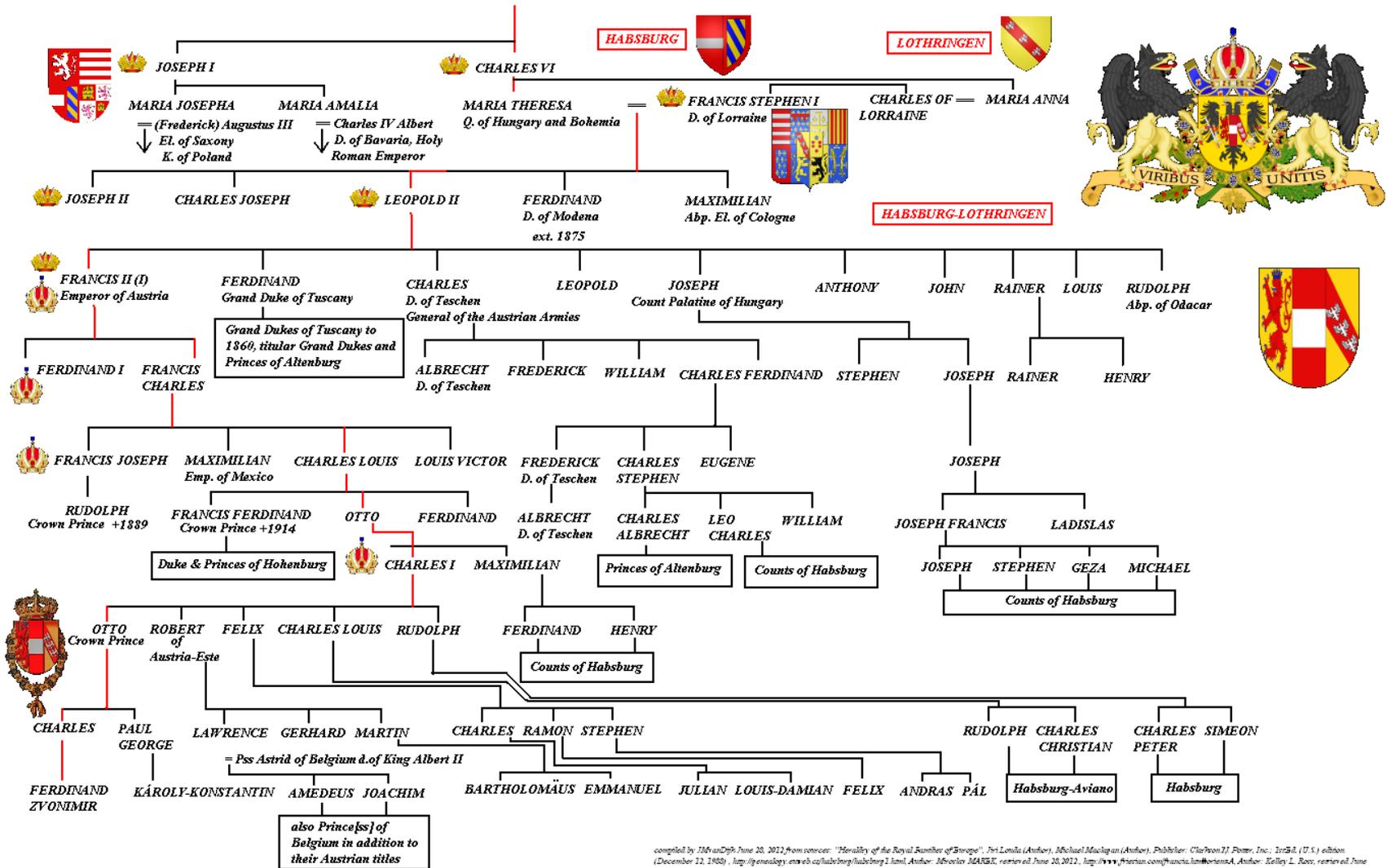
Breadths-first search (BFS)



Depth-first search (DFS)



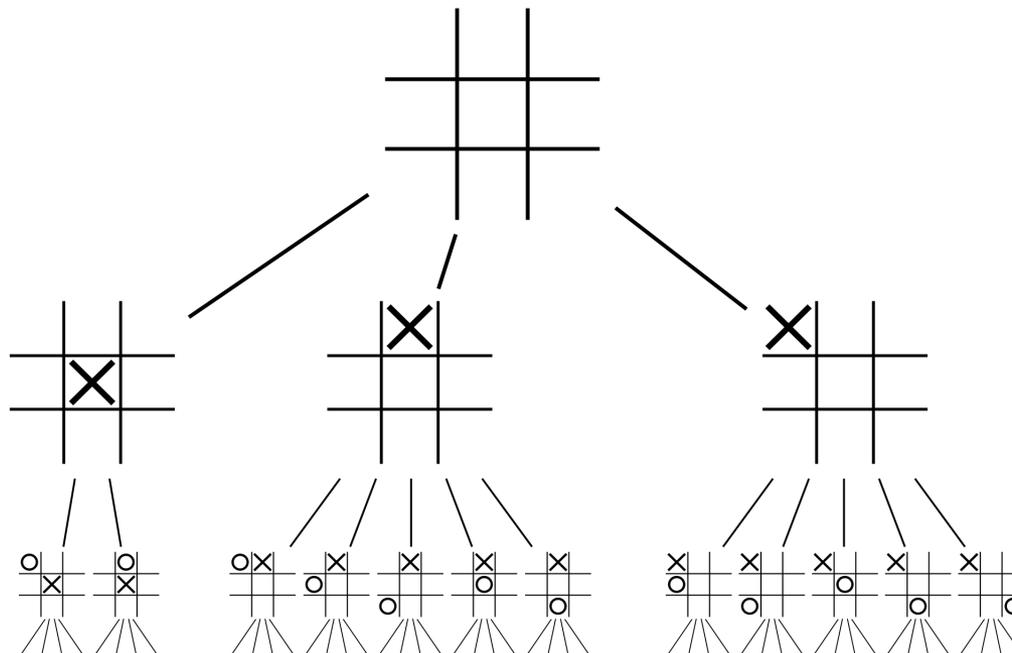
Ex.1: Habsburg Family Tree



compiled by: 2016 and 2017, from sources: "Heraldry of the Royal Families of Europe", Jiri Louda (Author), Michael Maclean (Author), Publisher: Clarendon Press, Inc., 1st Ed., (U.S.) edition (December 12, 1988), <http://genealogy.eth.edu/collections/habsburg1.html>, Author: Mervin MARGE, revised June 20, 2012, <http://www.fhstrian.com/fhstria.htm#habsburg>, Author: Kelly L. Ross, revised June 20, 2012, <http://www2.ica.int/ica/ship/genealogy/CBDOOM.html>, Author: Brian Tongue's Royal and Noble Genealogy, revised June 20, 2012, <http://royal.nyu.edu/~obrian/royal.html>, Bruce R. Gordon's Royal Chronology, revised June 20, 2012.

Game tree

- The number of **leaf nodes** is the number of possible different ways the game can be played
- tic-tac-toe has 255,168 leafs



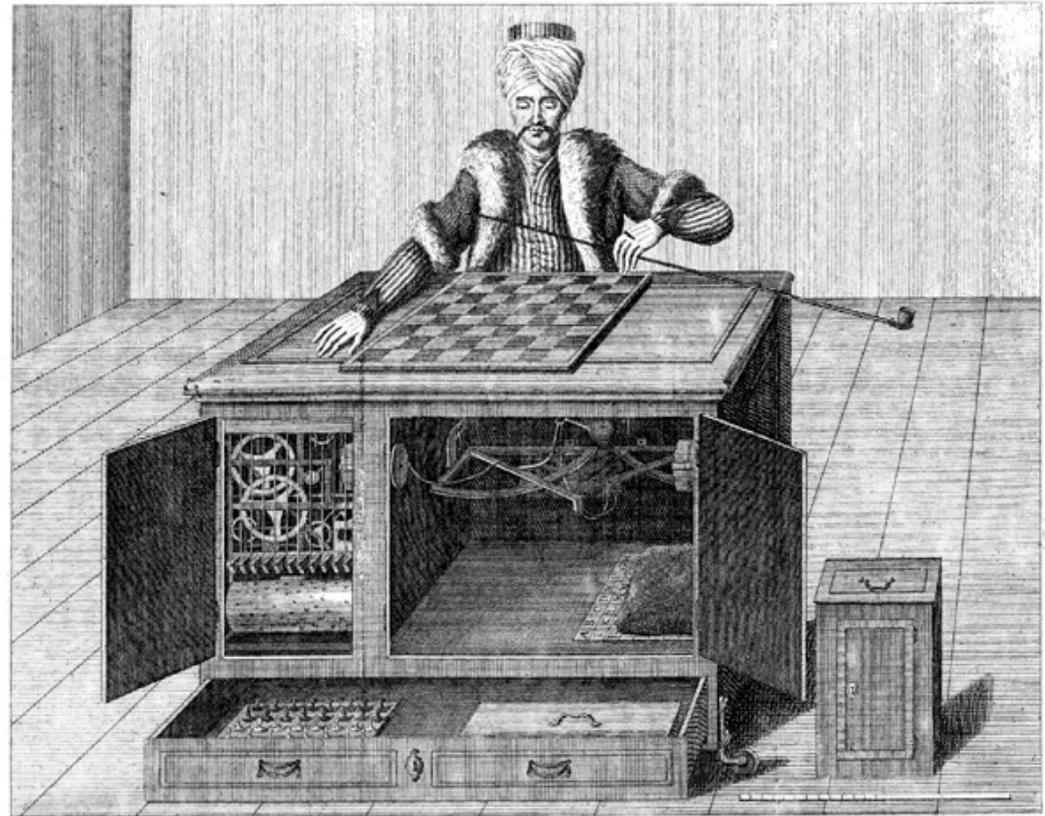
AI Games

Task	Year	Human	Machine	Method	Score
Chess	1997	Kasparov	IBM Deep Blue		2:1:3
Poker	2008	Grudzien	University of Alberta: Polaris 2.0	Learning	
Jeopardy	2011	Brad Rutter	IBM Watson	DeepQA	
Image recognition (ImageNet)	2015	Andrej Karpathy	Baidu Minwa	Neural network	95.42% : 95%
Go	2016	Lee Sedol	DeepMind: AlphaGo	Deep Learning + Monte Carlo tree search	4:1
Dota 2 1v1 International	2017	Dendi	OpenAI https://openai.com/the-international/		

<https://www.nature.com/nature/journal/v529/n7587/full/nature16961.html>

Mechanical Turk

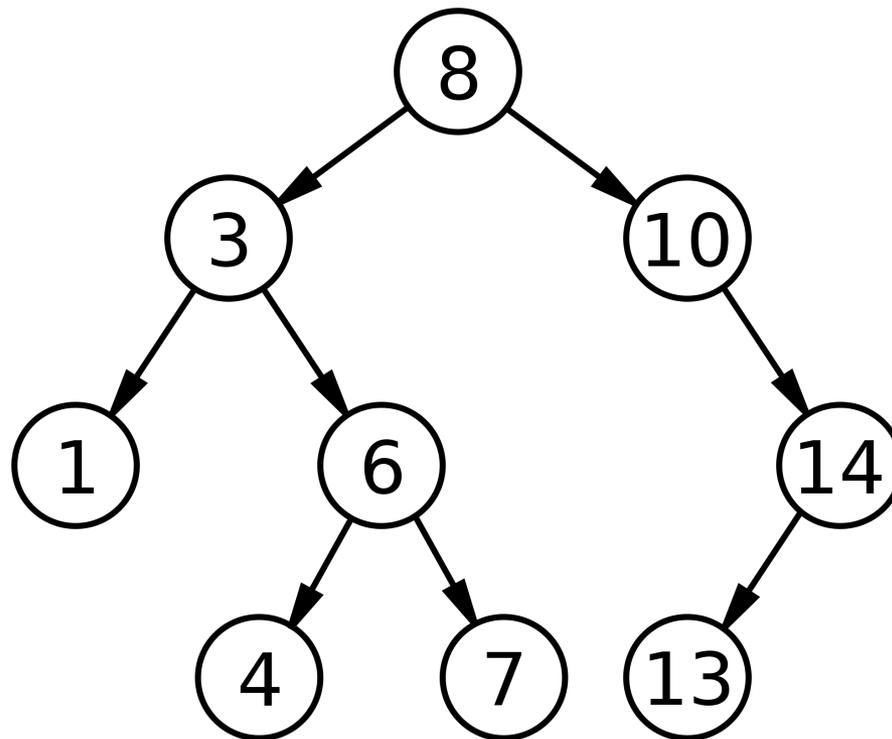
- Wolfgang von Kempelen
built in **Vienna** in **1770**
for Maria Theresa
- played chess
vs Napoleon Bonaparte
and Benjamin Franklin



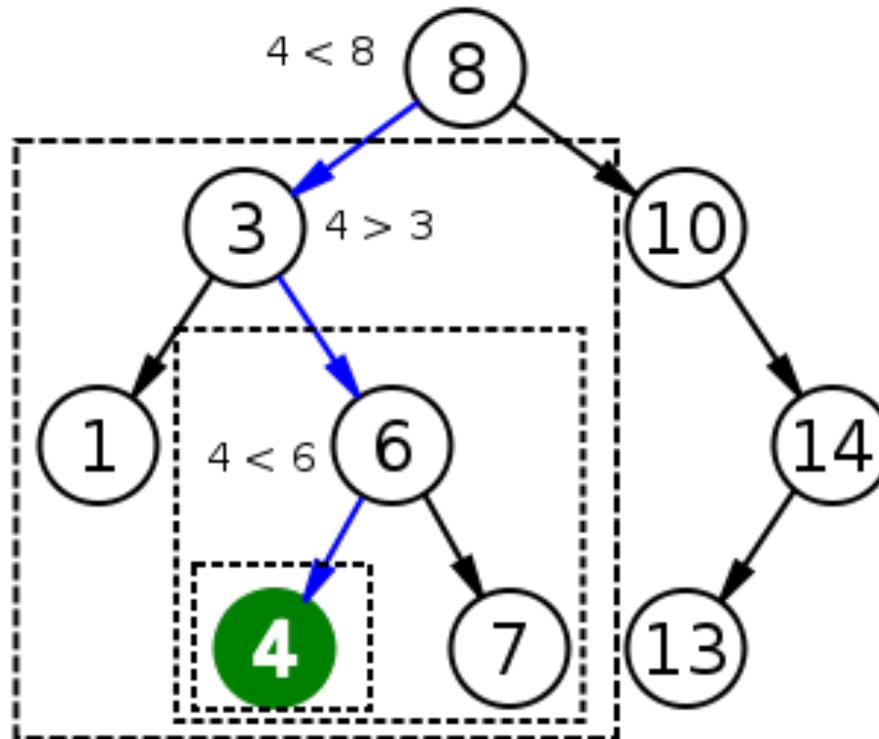
W. de Kempelen del. Che a Michel exaud. Basilea. P.G. Pütz, fecit.
Der Schachspieler, wie er vor dem Spiele gezeigt wird, von vorn. Le Joueur d'Échecs, tel qu'on le montre avant le jeu, par devant.

Binary tree

- maximum 2 children (left & right)



Binary search tree (BST)



$$h = O(\log n)$$

https://commons.wikimedia.org/wiki/File:Binary_search_tree_search_4.svg

<https://www.cs.cmu.edu/~adamchik/15-121/lectures/Trees/trees.html>

<https://medium.com/the-renaissance-developer/learning-tree-data-structure-27c6bb363051>

Binary search algorithm

```
def binary_search(item_list,item):
    first = 0
    last = len(item_list)-1
    found = False
    while( first<=last and not found):
        mid = (first + last)//2
        if item_list[mid] == item :
            found = True
        else:
            if item < item_list[mid]:
                last = mid - 1
            else:
                first = mid + 1
    return found

print(binary_search([1,2,3,5,8], 6))
print(binary_search([1,2,3,5,8], 5))
```

<http://interactivepython.org/runestone/static/pythonds/SortSearch/TheBinarySearch.html>

<https://www.w3resource.com/python-exercises/data-structures-and-algorithms/python-search-and-sorting-exercise-1.php>

https://en.wikipedia.org/wiki/Binary_search_algorithm

Recursive search

```
def binary_search_recursive(arr, elem, start=0, end=None):  
    if end is None:  
        end = len(arr) - 1  
    if start > end:  
        return False
```

```
    mid = (start + end) // 2  
    if elem == arr[mid]:  
        return mid  
    if elem < arr[mid]:  
        return binary_search_recursive(arr, elem, start, mid-1)  
    # elem > arr[mid]  
    return binary_search_recursive(arr, elem, mid+1, end)
```

Recursion



<https://xkcd.com/1557/>

Sort

- put elements of a **list** in a certain **order**
- output is a **permutation** (reordering with all of the original elements) of the input



https://commons.wikimedia.org/wiki/File:AZ_Sort.png



[https://de.wikipedia.org/wiki/Garderobe_\(Raum\)](https://de.wikipedia.org/wiki/Garderobe_(Raum))

Insert sort



<https://www.pexels.com/photo/game-deck-cards-shuffle-102107/>

Insert sort

```
def insertionsort(A):  
    for j in range(1, len(A)):  
        key = A[j]  
        i = j-1  
        while (i > -1) and key < A[i]:  
            A[i+1]=A[i]  
            i=i-1  
        A[i+1] = key  
    return A
```

<https://gist.github.com/basarat/3216903>

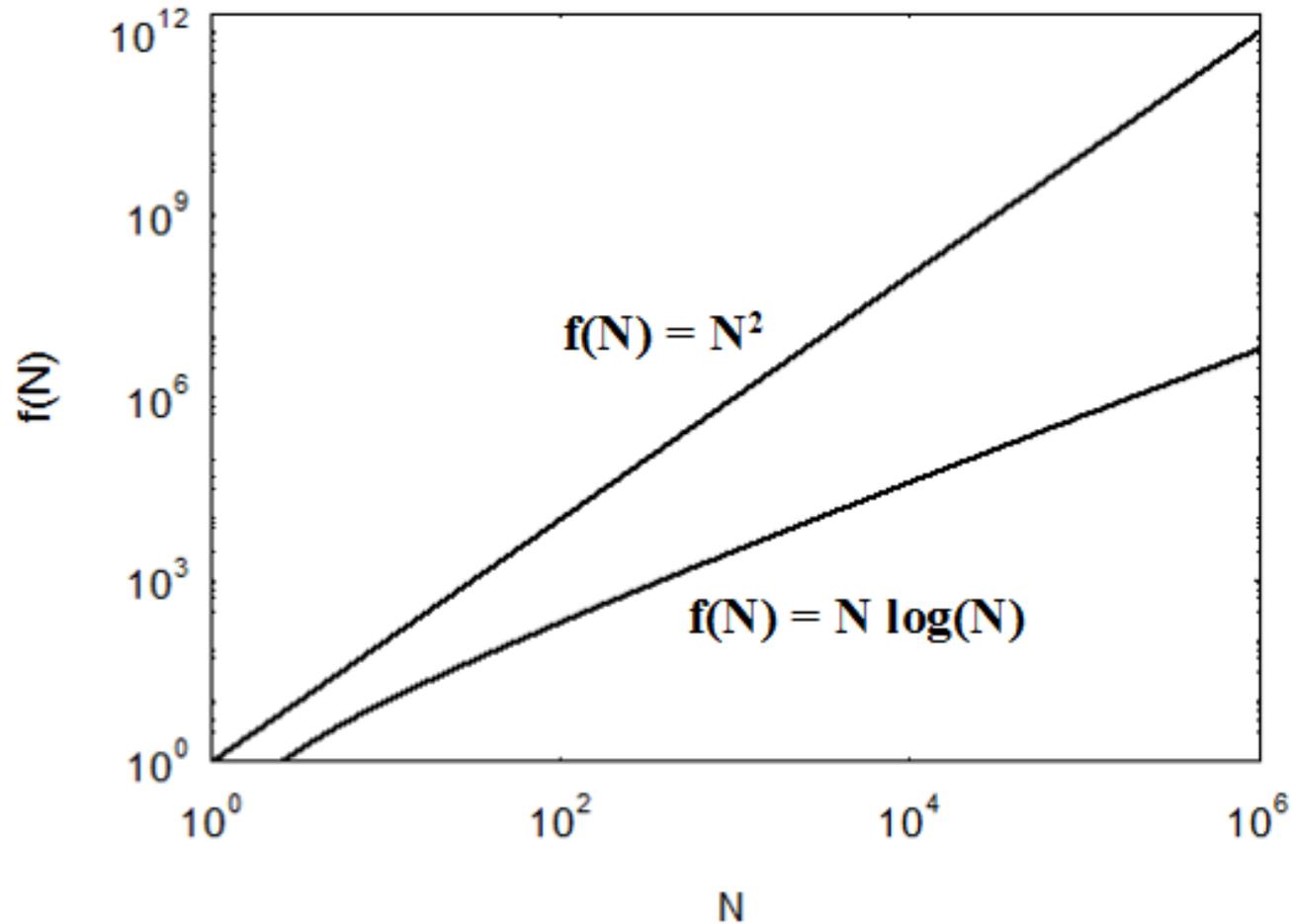
<http://interactivepython.org/courselib/static/pythonds/SortSearch/TheInsertionSort.html>

Insert sort

- best case $O(n)$: already sorted
- worst&average case $O(n*n)$: sorted in reverse order

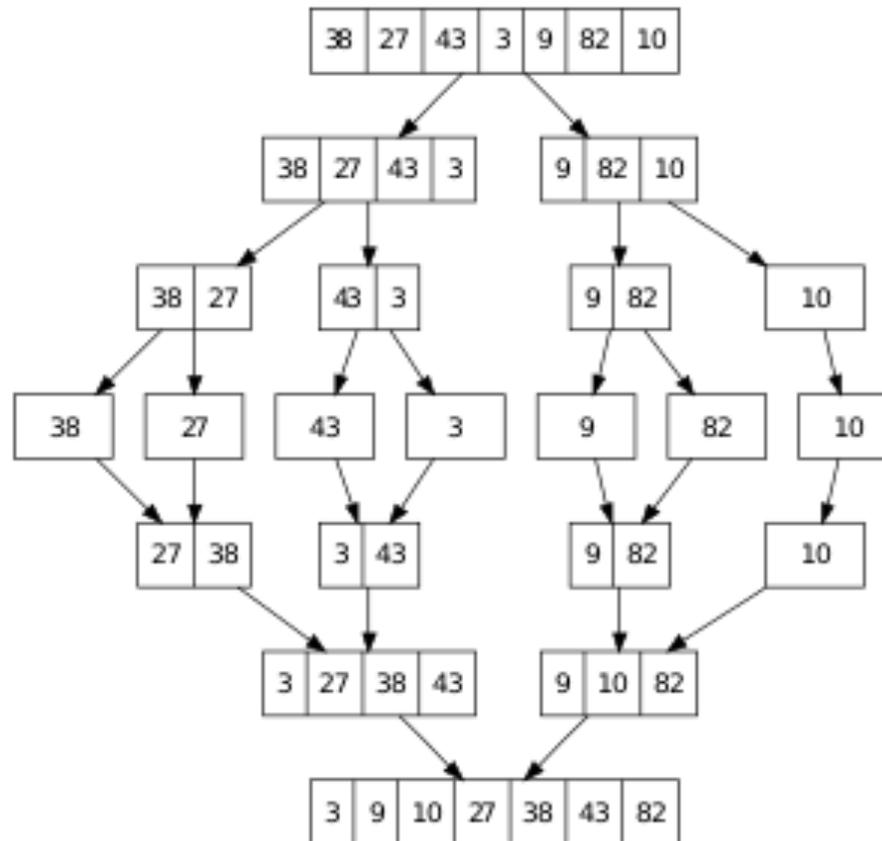
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            A[i+1]=A[i]  
            i=i-1  
        A[i+1] = key  
    return A
```

Big O Notation



Merge sort

- divide and conquer technique



https://en.wikipedia.org/wiki/Merge_sort

Merge sort with saxon folk dance: https://www.youtube.com/watch?v=XaqR3G_NVoo

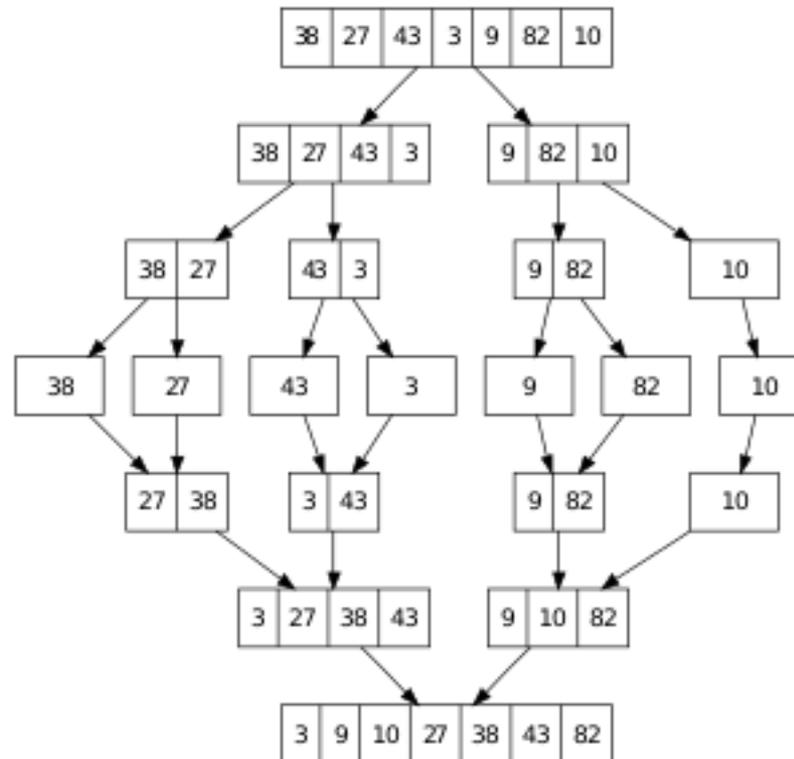
Merge sort

- **recursively** dividing list into smaller sublists which are then sorted

```
def mergesort(list):  
    if len(list) < 2:  
        return list  
  
    middle = len(list)/2  
  
    left = mergesort(list[:middle])  
    right = mergesort(list[middle:])  
  
    return merge(left, right)
```

Merge sort

- worst-case running time is $O(n \log n)$



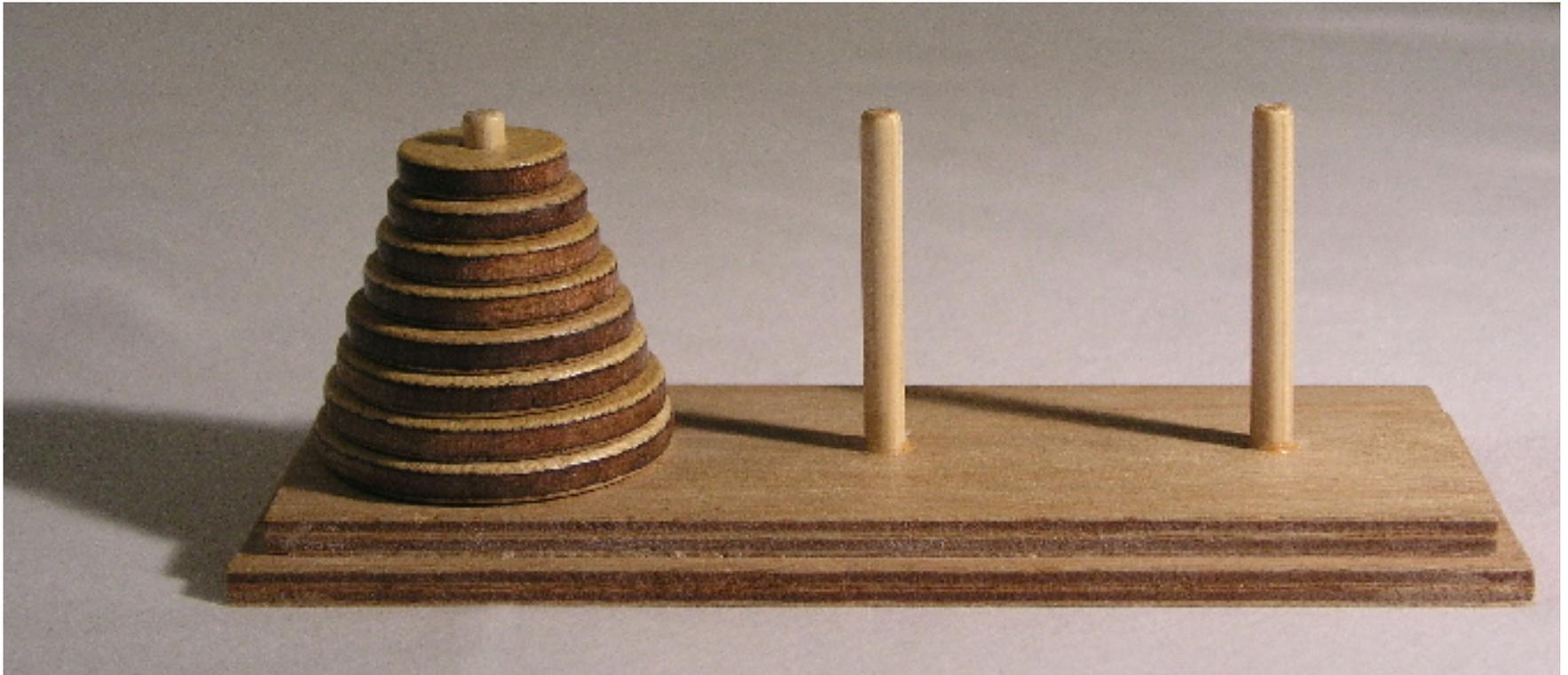
https://en.wikipedia.org/wiki/Merge_sort

Ex.3: Palindrome

- Sator Square: "Sator Arepo Tenet Opera Rotas"
- "The sower Arepo holds with effort the wheels"



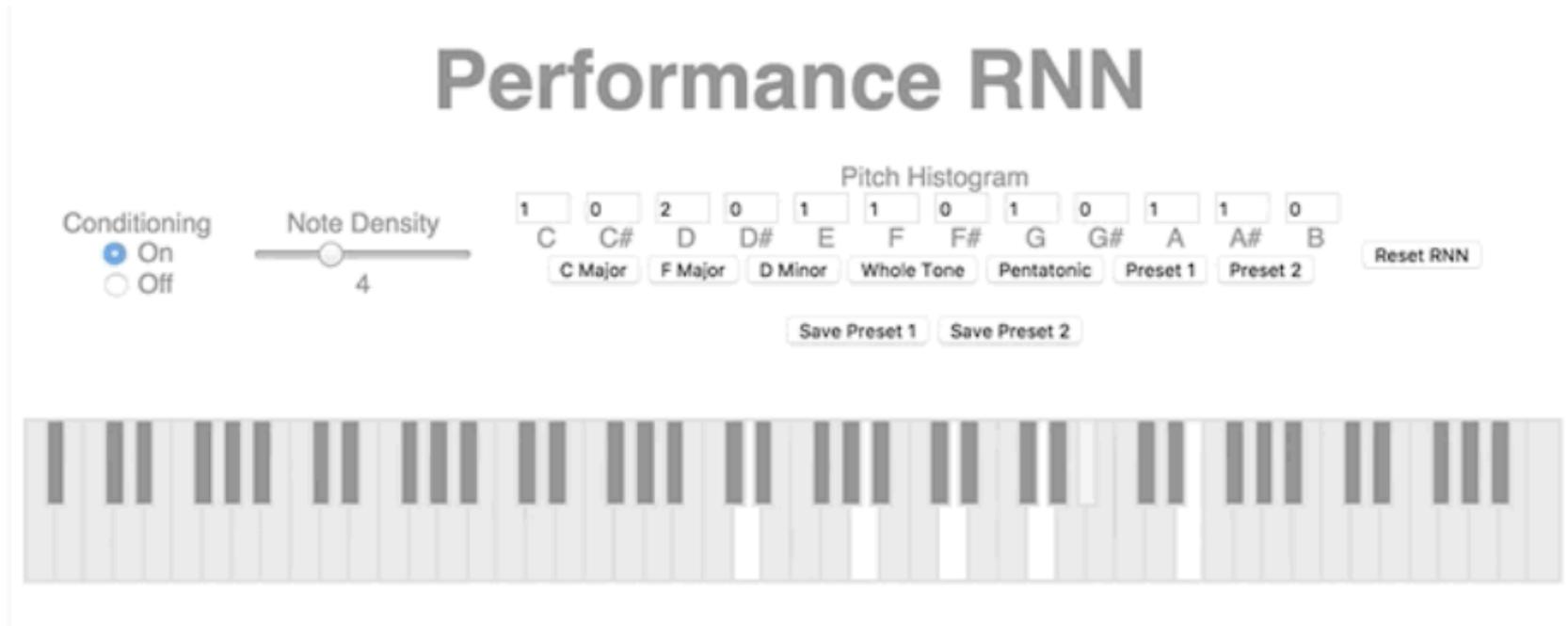
Ex.4: Tower of Hanoi



https://commons.wikimedia.org/wiki/File:Tower_of_Hanoi.jpeg

Machine Learning

- model trained on ~1400 performances by skilled pianists
https://deeplearnjs.org/demos/performance_rnn



<https://magenta.tensorflow.org/performance-rnn-browser>

<https://github.com/AlexiaJM/Deep-learning-with-cats>

<https://machinelearningmastery.com/text-generation-lstm-recurrent-neural-networks-python-keras/>

Thank you!

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